

# From Dynamics to Thermodynamics using Molecular Simulation



David van der Spoel

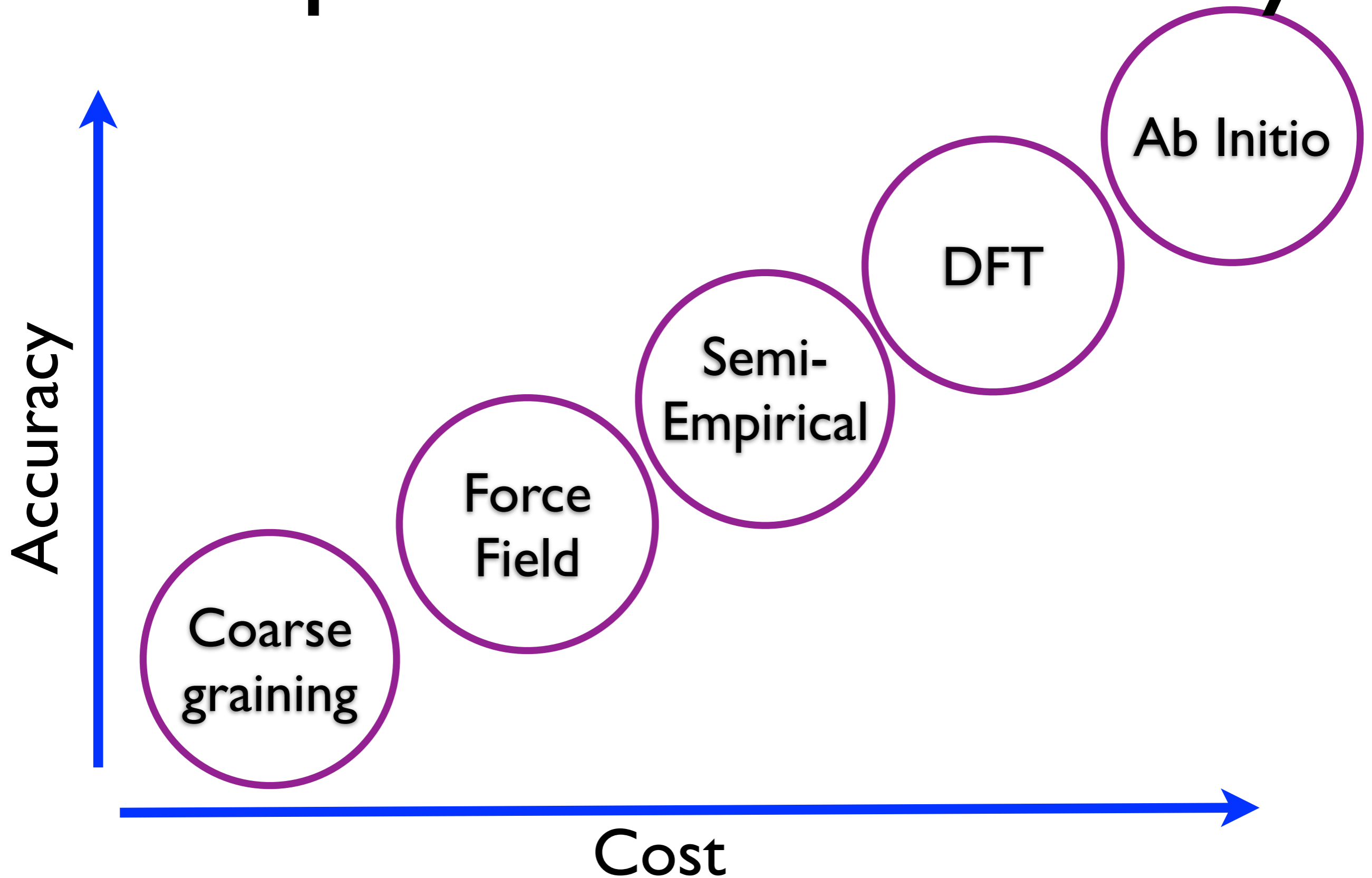
# Computational Chemistry

- \* Physical models to describe molecules
- \* Software to evaluate models and do predictions - GROMACS
- \* Model validation and development
- \* Applications in Chemistry - Water & other liquids
- \* (Applications in Biology - PitGP, Virus, Malaria)

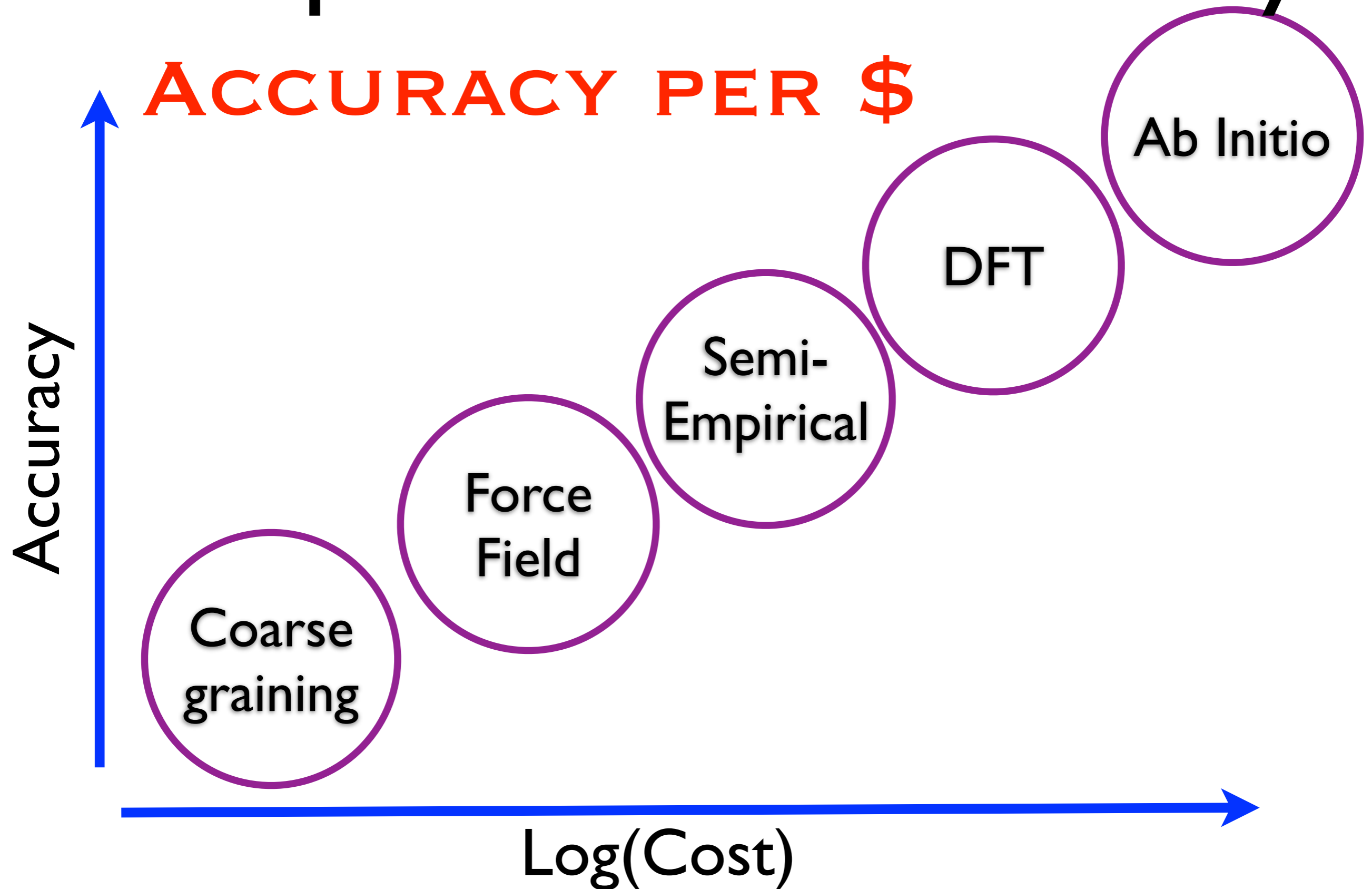
# Computational Chemistry

- \* Ab-initio methods
- \* Density functional theory
- \* Semi-empirical
- \* Atomistic Force field
- \* Coarse grained FF / QSAR / Continuum descriptions

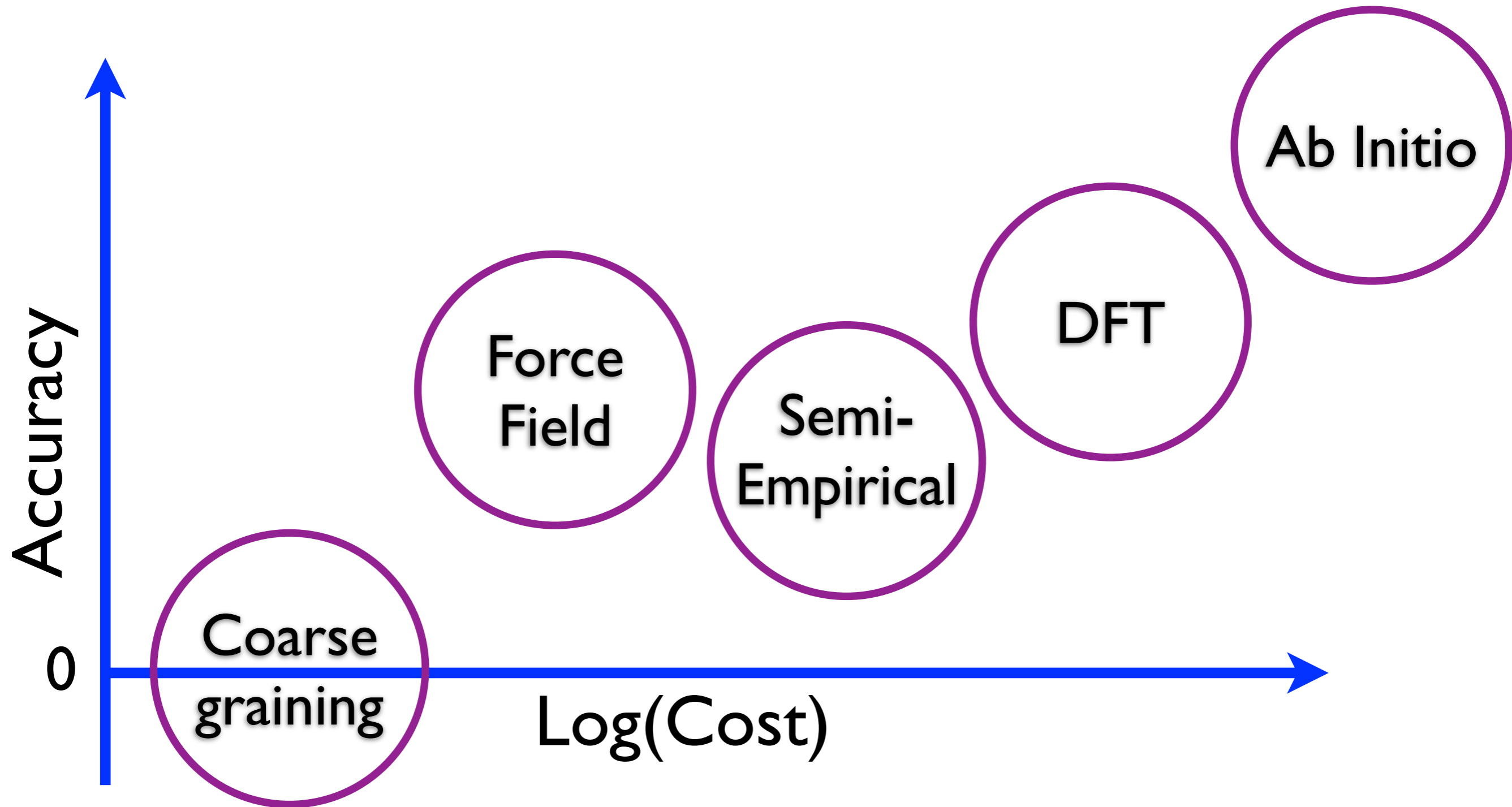
# Computational Chemistry



# Computational Chemistry



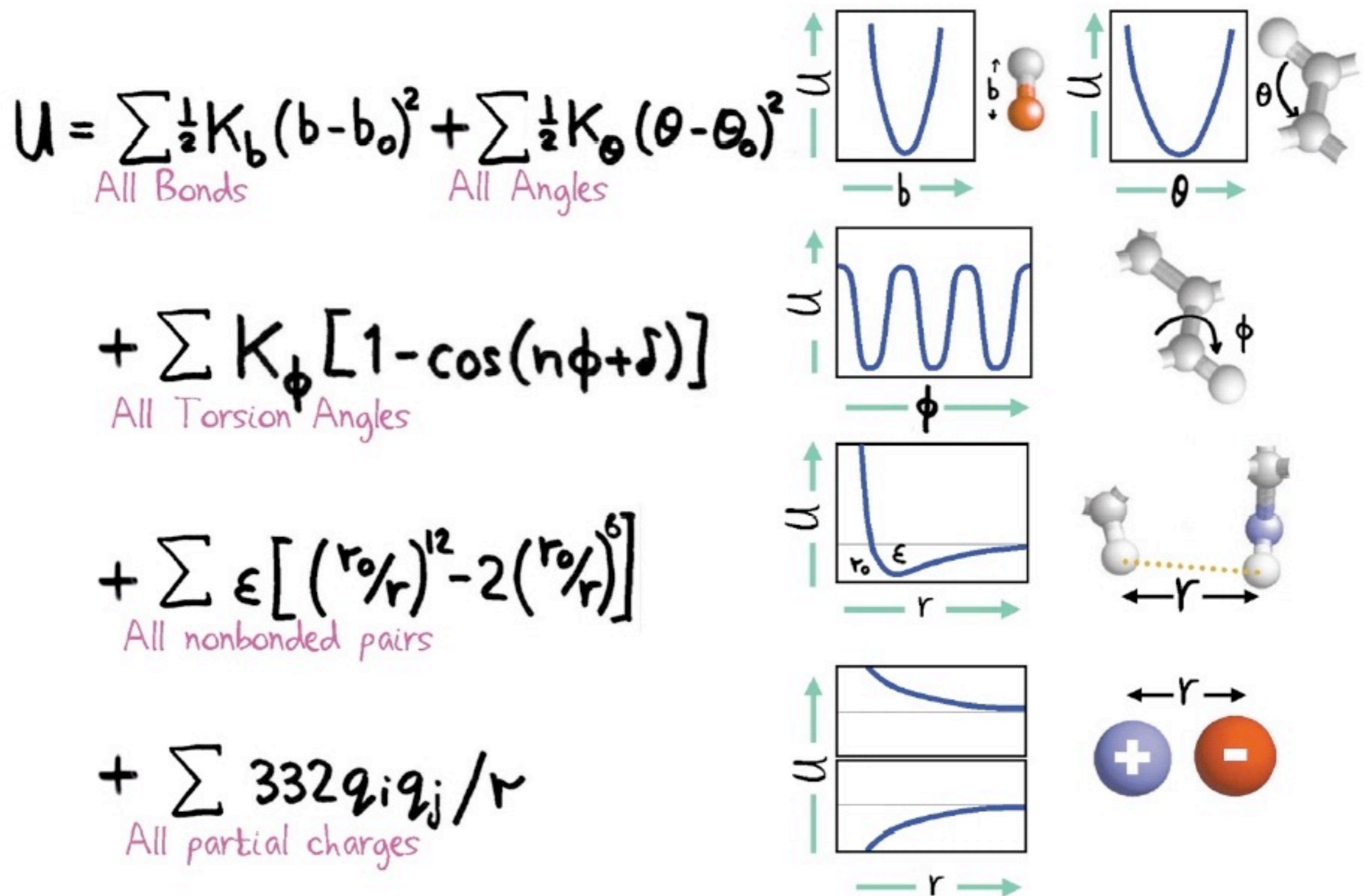
# Computational Chemistry



**Depends on the problem!**

# What is Molecular Dynamics

- Coordinates of atoms/particles as a function of time
- Time correlation functions
- Experimental: Nuclear Magnetic Resonance spectroscopy
- Computer simulations at different levels of spatial and temporal accuracy
- Sampling the conformational space - partition function



**Fig. 1** The total potential energy of any molecule is the sum of terms allowing for bond stretching, bond angle bending, bond twisting, van der Waals interactions and electrostatics. Many properties of a biomolecules can be simulated with such an empirical energy function.

M.Levitt, Nat. Struct. Biol. 8 (2001), p. 392-393

# How Many Lennard-Jones Parameters for a Protein?

- \* Two parameters per interaction
- \* One atom type per element (C,H,N,O,S) : 10 with combination rules, 40 without
- \* With four atom types per element: 40 with combination rules, 760 without

# The Physical Model

- \* What determines the quality?
- \* How can we test it?

# Our Gr8t Software

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Sök



David van der Spoel

Hitta vänner

Startsida



## GROMACS

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GROMACS · Alla (senaste) ▾

Dela: [Inlägg](#) [Foto](#) [Länk](#)

Skriv något...



**Navid Zolfaghari**

I wonder to see if any workshop is going to be held in U.S.

[Gilla](#) · [Kommentera](#) · den 10 februari kl. 19:14



**Santosh Kumar**

Can anyone tell that how to add the new residue in the forcefield in gromacs ? is the any tutorial for this???

[Gilla](#) · [Kommentera](#) · den 8 februari kl. 19:56



**Thanos Tequila**

Hi gromacs users,  
I have some trouble trying to complie gromacs on a GPU. Is there an easy, step by step, guide to help me complete this process? :))  
thanks

[Gilla](#) · [Kommentera](#) · den 4 februari kl. 18:09



**Neshat Haq**

Hi gromacs users ,  
Can anyone tell, what are the considerations to be kept in mind while going for a metalloprotein simulation, like protein containing Fe<sup>3+</sup> and Mn<sup>2+</sup> ions.  
Or is there any tutorial describing the steps, in your knowledge.

[Gilla](#) · [Kommentera](#) · den 31 januari kl. 11:00



**Donal Murphy**

If you're using GPUs in your work and want to share exciting new

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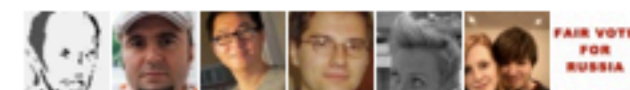
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Du och GROMACS



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cdon.se



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**Stockholm!**

groupon.se



Upplev de 5 roligaste aktiviteterna i Stockholm.

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GROMACS is a software package for simulations of molecular dynamics.

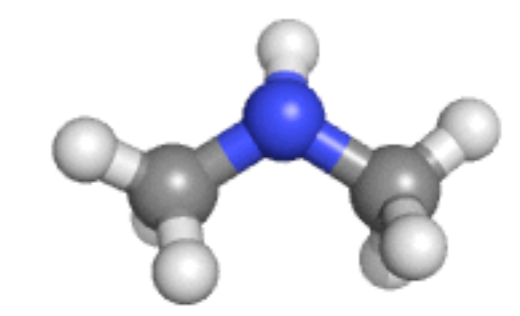
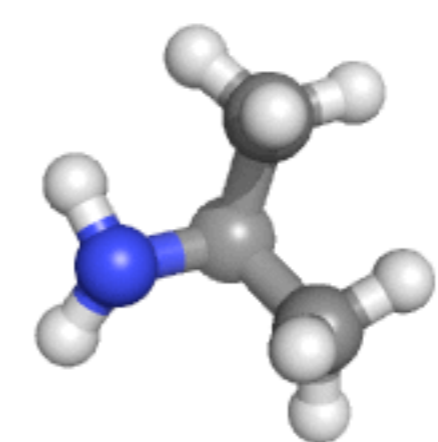
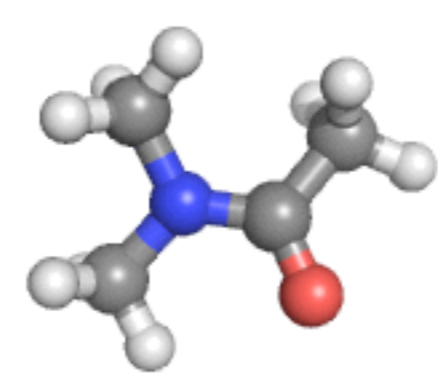
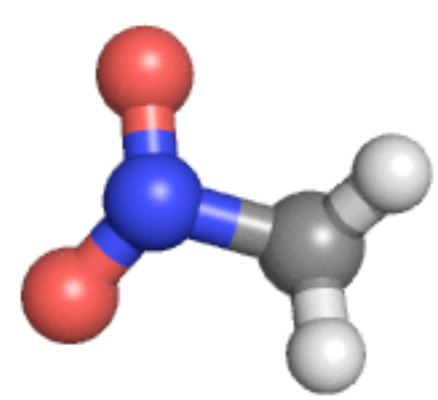
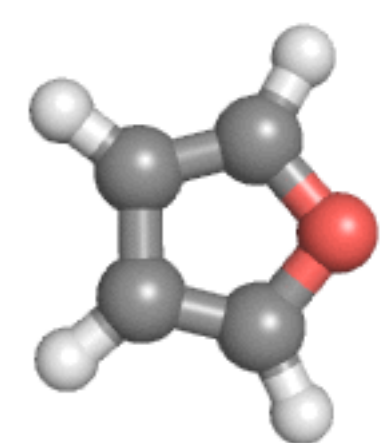
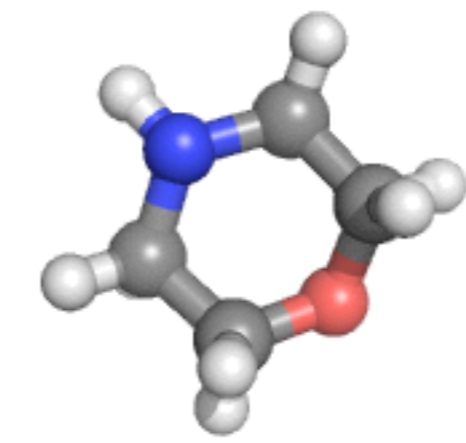
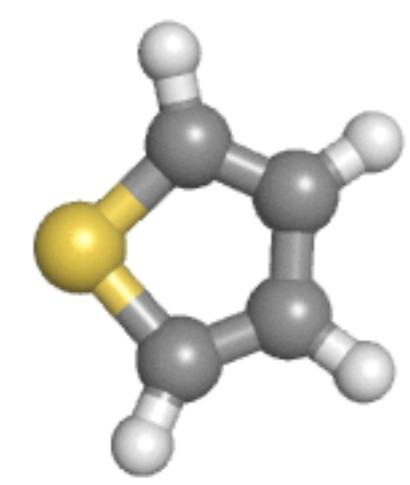
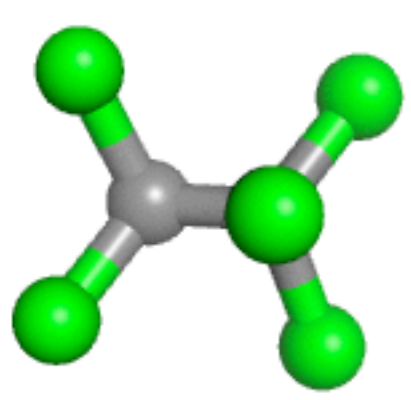
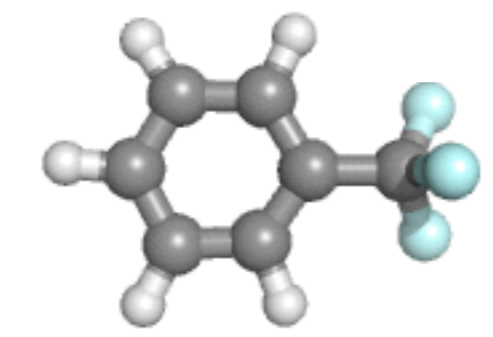
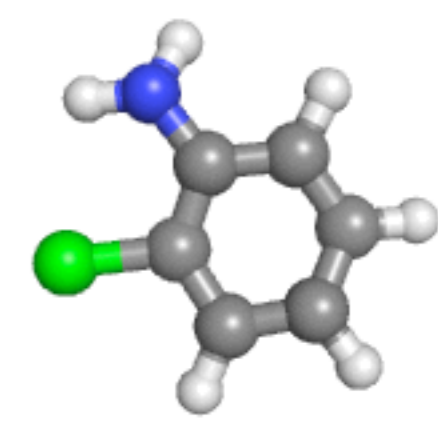
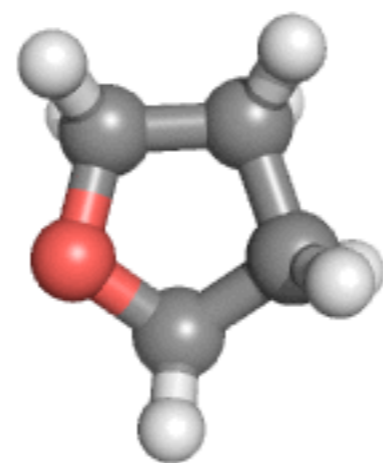
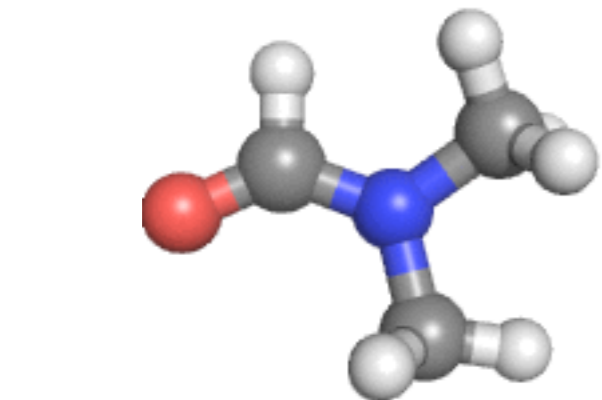
**481**

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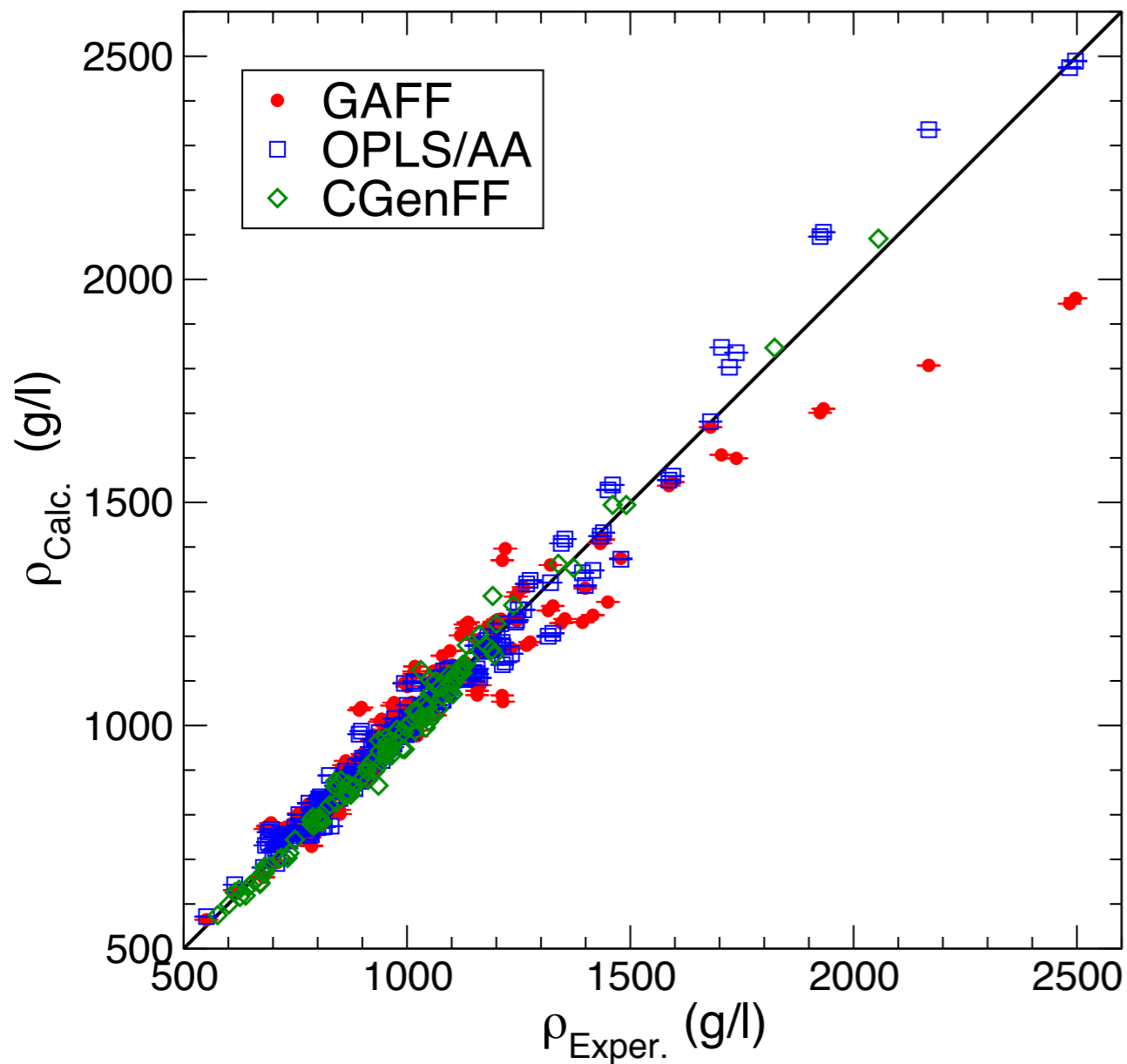
<http://www.gromacs.org>

# Liquid FF Benchmark

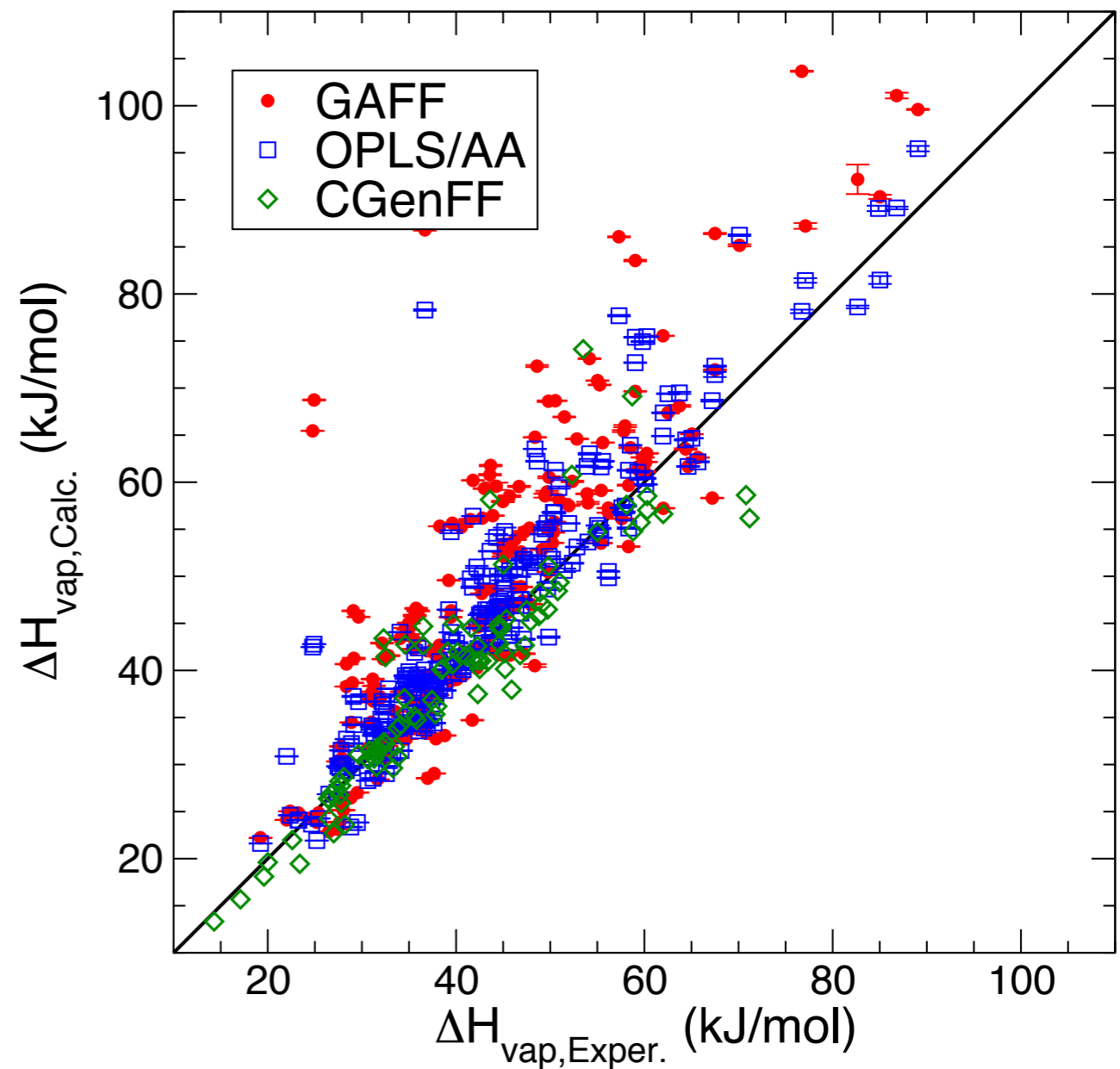
- Test available force field for how good they reproduce properties for ~ 150 organic liquids
- 1000 molecules/box 10 ns production sims
- OPLS/AA, GAFF + CGenFF from literature



# Simple props



Density

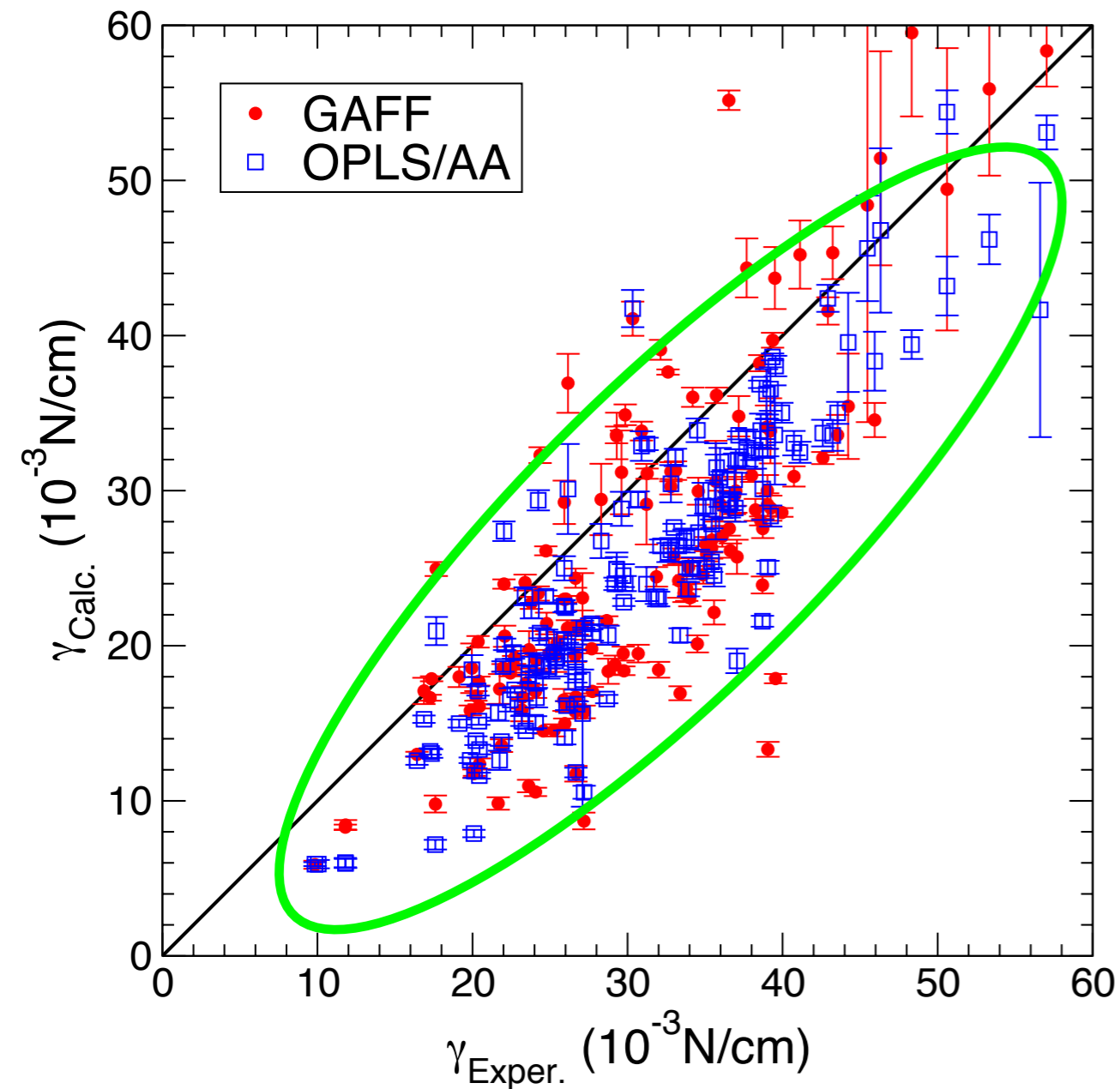


Enthalpy of Vaporization

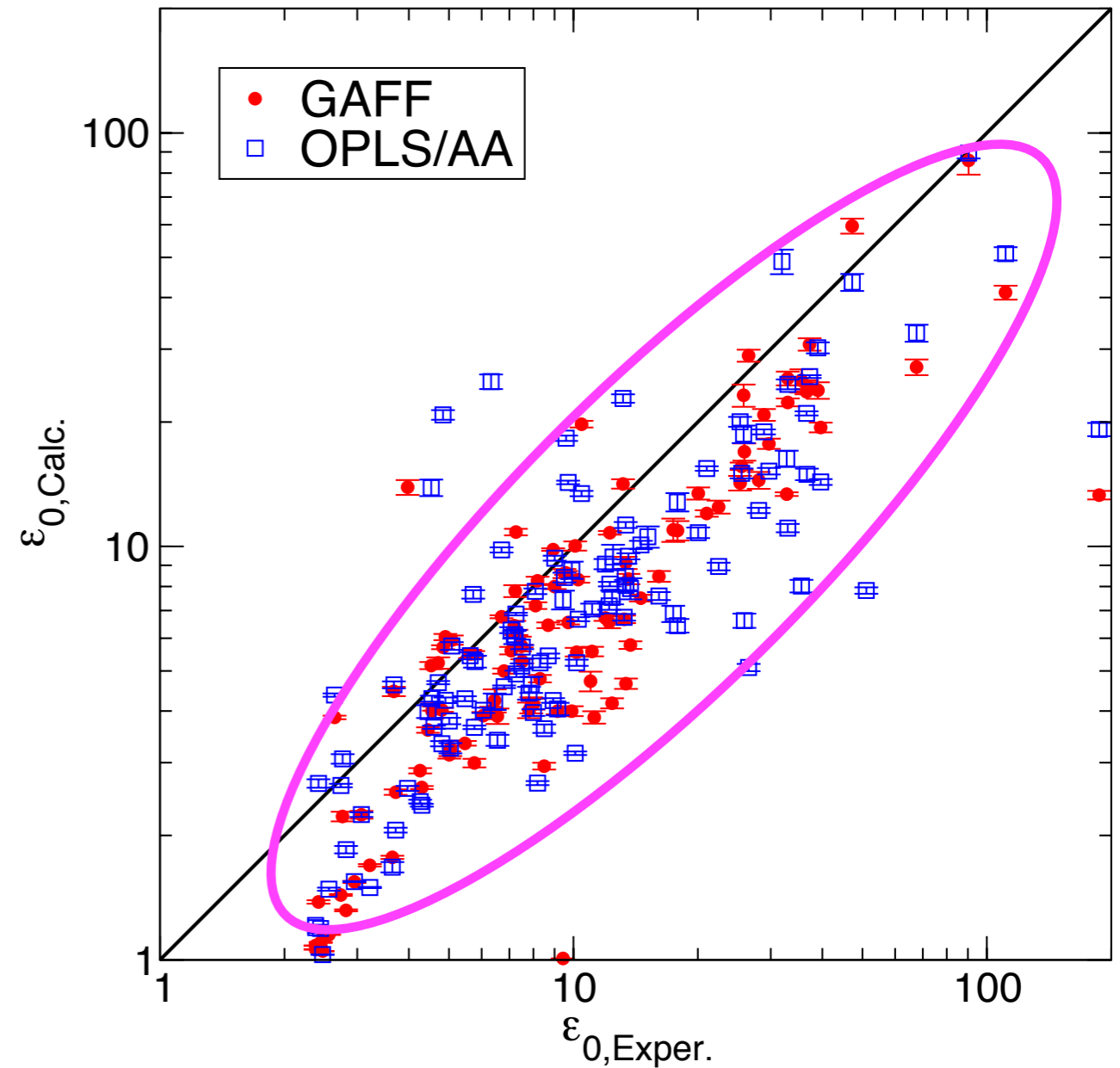
# Not so simple props

Due to cut-off of Van der Waals forces?

Polarization?



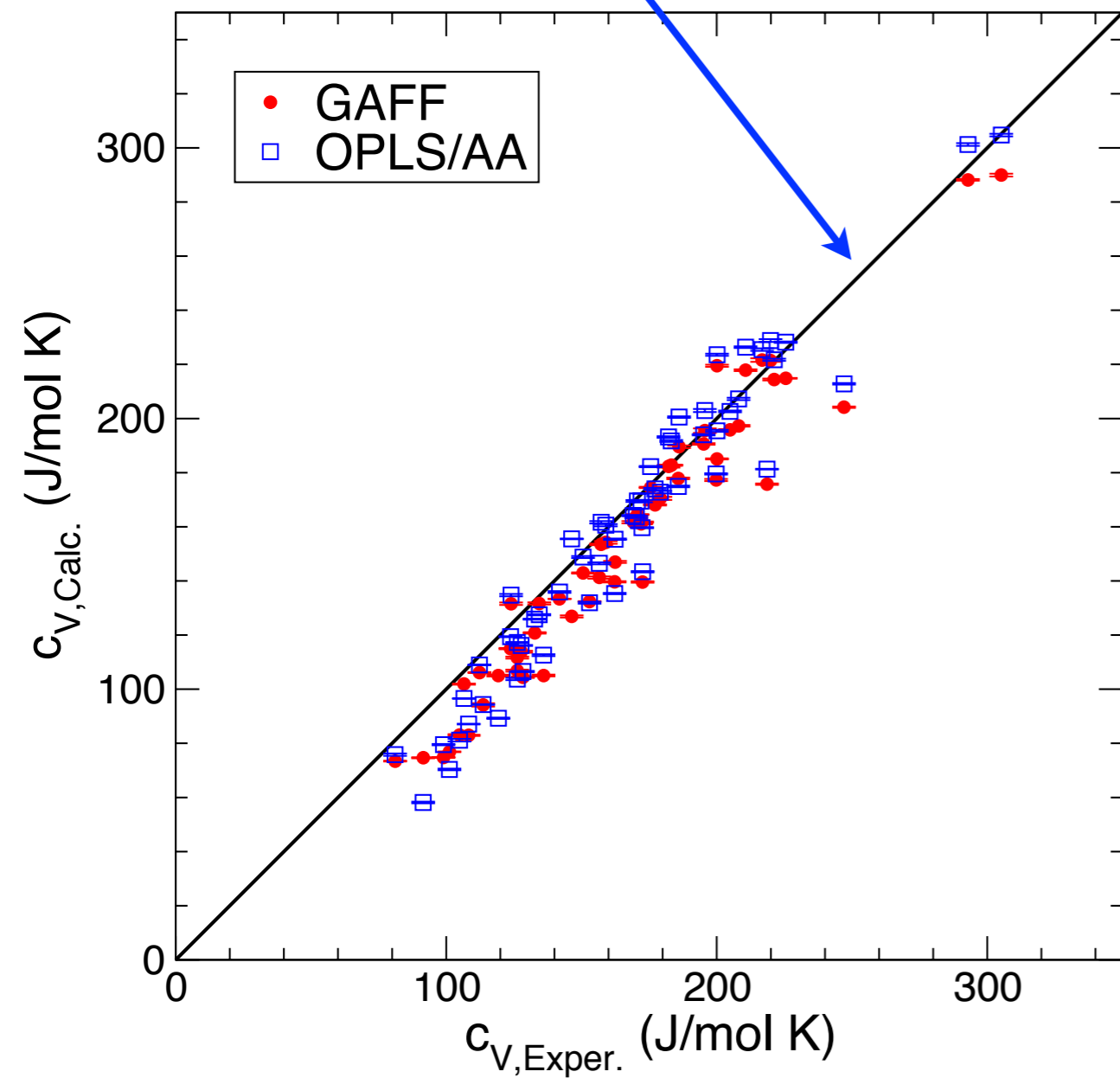
Surface Tension



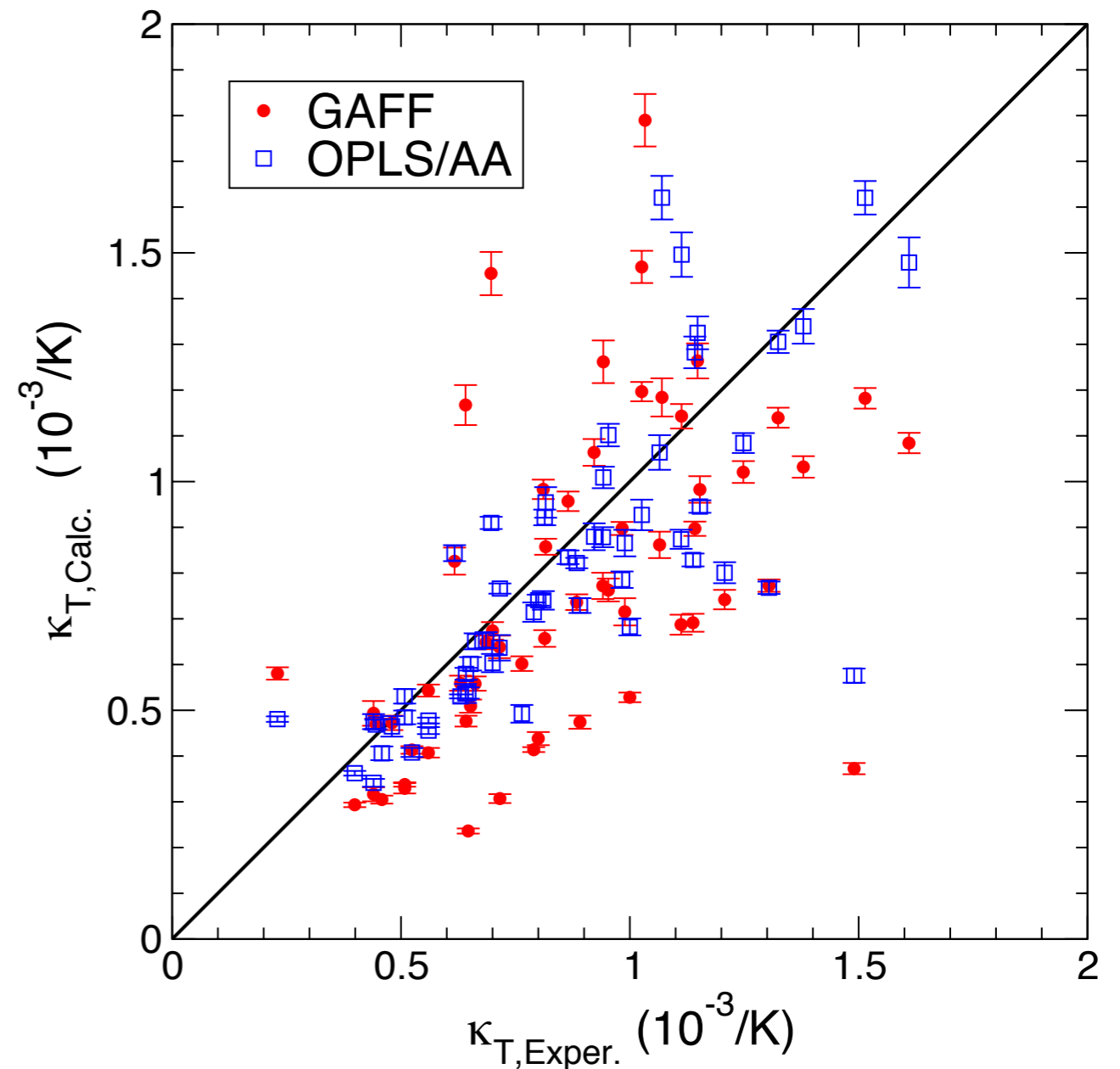
Dielectric Constant

## 2 Phase Thermodynamics method!

# Complex props



Heat capacity



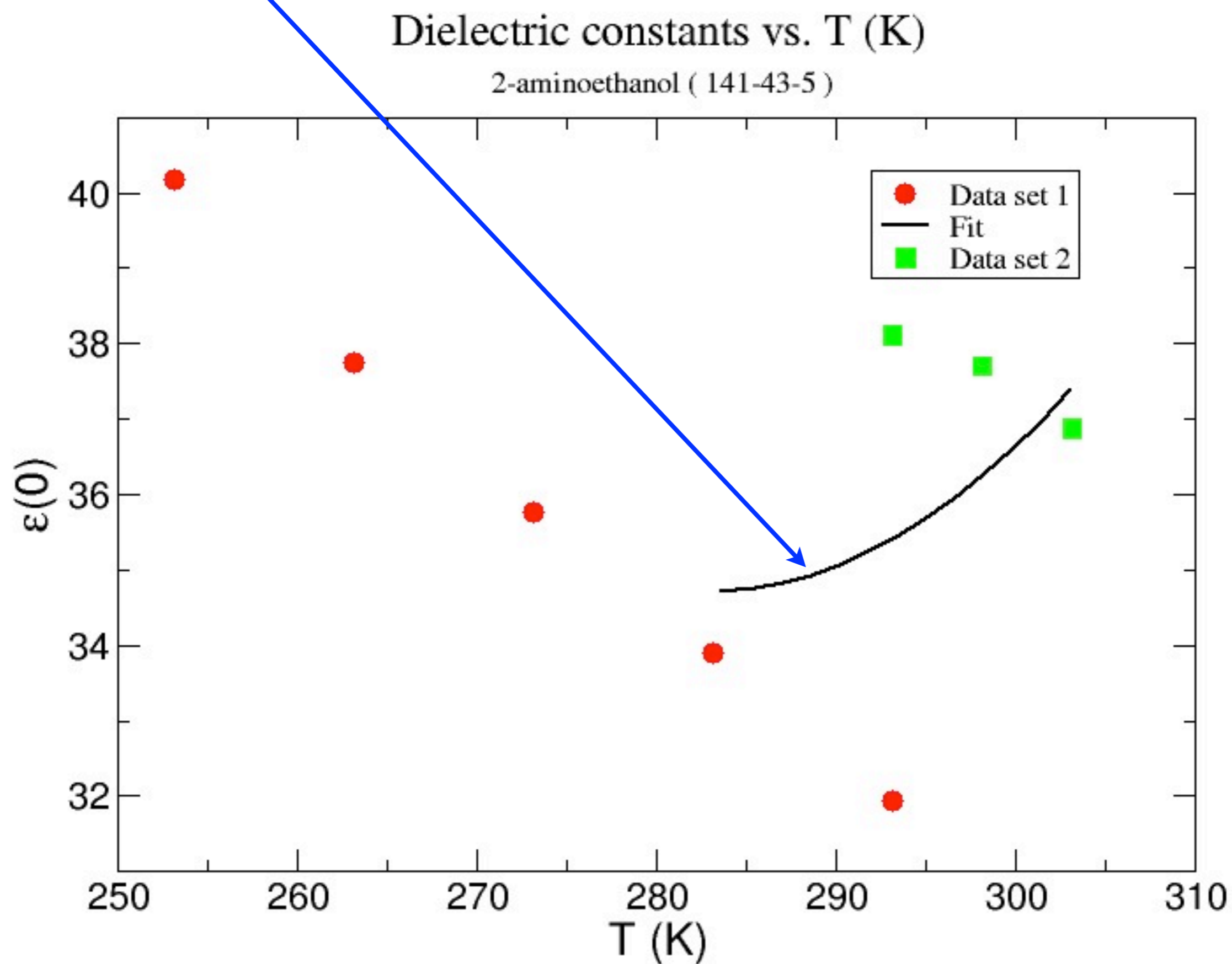
Compressibility

# Yihzak Marcus: The Properties of Solvents

**Table 3.1** Thermophysical properties of solvents (temperature dependent properties at 25°C, unless otherwise noted)

No	Name	M	T <sub>m</sub>	T <sub>b</sub>	T <sub>c</sub>	d	V	$\alpha_p$	$\kappa_T$	$\rho$	dH <sub>v</sub>	$\delta$	C <sub>p</sub>
0	vacuum	0.00				0.0000 j	0.0						0.00 j
10	tetramethylsilane	88.23	174.1 [1]	299.8 [1]	450.4 [2]	0.6464 [1]	136.5	1.84 [2]	2.884 [gg]	9.56E+01 [1]	24.20 [1]	12.6	204.1 [1]
20	n-pentane	72.15	143.4 [1]	309.2 [1]	496.7 [1]	0.6214 [1]	116.1	1.58 [1]	2.180 [1]	6.87E+01 [1]	26.41 [1]	14.4	167.1 [1]
30	2-methylbutane	72.15	113.3 [1]	301.0 [1]	460.4 [1]	0.6140 [1]	117.5	1.66 [1]	2.450 [1]	9.17E+01 [1]	24.84 [1]	13.8	165.4 [1]
40	n-hexane	86.18	177.8 [1]	341.9 [1]	507.7 [1]	0.6549 [1]	131.6	1.39 [1]	1.706 [1]	2.02E+01 [1]	31.48 [1]	15.0	195.4 [1]
50	c-hexane	84.16	279.9 [1]	353.9 [1]	553.6 [1]	0.7742 [1]	108.7	1.23 [1]	1.140 [1]	1.30E+01 [1]	32.89 [1]	16.8	156.0 [1]
60	n-heptane	100.2	182.6 [1]	371.6 [1]	540.7 [1]	0.6793 [1]	147.5	1.27 [1]	1.442 [1]	6.10E+00 [1]	36.58 [1]	15.2	224.9 [1]
70	n-octane	114.2	216.4 [1]	398.8 [1]	568.8 [1]	0.6987 [1]	163.5	1.17 [1]	1.282 [1]	1.87E+00 [1]	41.49 [1]	15.5	254.1 [1]
80	2,2,4-trimethyl pentane	114.2	165.8 [1]	372.4 [1]	543.9 [1]	0.7122 [1]	160.4	1.20 [1]		6.50E+00 [1]	35.15 [1]	14.7	238.5 [1]
90	n-decane	142.2	243.5 [1]	447.3 [1]	617.6 [1]	0.7263 [1]	195.9	1.05 [1]	1.093 [1]	1.80E-01 [1]	51.38 [1]	15.8	314.5 [1]
100	n-dodecane	170.3	263.6 [1]	489.5 [1]	658.3 [1]	0.7541 [1]	228.6	0.98 [1]	0.989 [1]	1.50E-01 [1]	61.29 [1]	16.0	375.9 [1]
110	n-hexadecane	226.4	291.0 [3]	560.0 [3]	720.6 [2]	0.7700 [1]	294.1	0.88 [1]	0.867 [3]	2.00E-04 [1]	81.09 [1]	16.3	501.4 [2]
120	benzene	78.12	278.7 [1]	353.2 [1]	562.2 [1]	0.8690 [1]	89.9	1.23 [1]	0.962 [1]	1.27E+01 [1]	33.85 [1]	18.8	135.7 [1]
130	toluene	92.14	178.2 [1]	383.8 [1]	591.8 [1]	0.8619 [1]	106.9	1.07 [1]	0.922 [1]	3.75E+00 [1]	37.99 [1]	18.8	157.2 [1]
140	o-xylene	106.1	248.0 [1]	417.6 [1]	630.3 [1]	0.8760 [1]	121.2	0.95 [1]	0.811 [1]	8.80E-01 [1]	43.43 [1]	18.0	188.0 [1]
150	m-xylene	106.1	225.3 [1]	412.3 [1]	617.1 [1]	0.8604 [1]	123.4	0.99 [1]	0.862 [1]	1.10E+00 [1]	42.66 [1]	18.0	183.4 [1]
160	p-xylene	106.1	286.4 [1]	411.5 [1]	616.2 [1]	0.8569 [1]	123.9	1.00 [1]	0.859 [1]	1.17E+00 [1]	42.38 [1]	18.1	181.6 [1]
170	ethylbenzene	106.1	178.2 [1]	409.3 [1]	617.2 [1]	0.8625 [1]	123.1	1.02 [1]	0.865 [1]	1.30E+00 [1]	42.25 [1]	18.0	185.5 [1]
180	cumene	120.1	177.1 [1]	425.6 [1]	631.1 [1]	0.8573 [1]	140.2	0.98 [1]	0.893 [1]	6.10E-01 [1]	45.14 [1]	17.6	198.9 [1]
190	mesitylene	120.1	228.4 [1]	437.9 [1]	637.3 [1]	0.8610 [1]	139.6	0.94 [1]	0.699 [1]	3.30E-01 [1]	7.48 [1]	18.1	209.1 [1]
200	styrene	104.1	242.5 [1]	418.3 [1]	636.9 [1]	0.9010 [1]	115.6	0.97 [1]		8.40E-01 [1]	43.93 [1]	18.9	182.5 [1]
210	tetralin	132.2	237.4 [1]	480.8 [1]	754.0 [1]	0.9657 [1]	136.9	0.72 [1]		5.30E-02 [1]	55.23 [1]	19.4	217.4 [1]
220	cis-decalin	138.2	230.1 [1]	468.9 [1]	702.2 [1]	0.8931 [1]	154.8	0.85 [1]		1.00E-01 [1]	51.34 [1]	17.8	232.0 [1]
230	water	18.02	273.2 [1]	373.2 [1]	647.1 [1]	0.9974 [1]	18.1	0.26 [1]	0.457 [1]	3.17E+00 [1]	43.91 [1]	47.9	75.30 [1]
240	methanol	32.04	175.5 [1]	337.7 [1]	512.6 [1]	0.7872 [1]	40.7	1.19 [1]	1.248 [1]	1.69E+01 [1]	37.43 [1]	29.3	81.47 [1]
250	ethanol	46.07	158.7 [1]	351.4 [1]	513.9 [1]	0.7848 [1]	58.7	1.09 [1]	1.153 [1]	7.89E+00 [1]	42.32 [1]	26.0	112.3 [1]
260	n-propanol	60.10	147.0 [1]	370.3 [1]	537.3 [1]	0.8003 [1]	75.1	1.01 [1]	1.025 [1]	2.73E+00 [1]	47.45 [1]	24.4	143.8 [1]
270	i-propanol	60.10	185.2 [1]	355.4 [1]	508.3 [1]	0.7815 [1]	76.9	1.08 [1]	1.332 [1]	6.03E+00 [1]	45.39 [1]	23.7	154.6 [1]
280	n-butanol	74.12	184.5 [1]	390.8 [1]	563.0 [1]	0.8057 [1]	92.0	0.93 [1]	0.941 [1]	8.20E-01 [1]	52.35 [1]	23.3	177.0 [1]
290	i-butanol	74.12	165.0 [1]	381.0 [1]	547.8 [1]	0.7978 [1]	92.9	0.98 [1]	1.026 [1]	1.38E+00 [1]	50.82 [1]	22.9	181.0 [1]
300	2-butanol	74.12	158.5 [1]	372.7 [1]	536.0 [1]	0.8030 [1]	92.3	1.06 [1]	0.983 [7]	2.43E+00 [1]	49.72 [1]	22.6	213.8 [1]
310	t-butanol	74.12	298.8 [1]	355.5 [1]	506.2 [1]	0.7810 [1]	94.9	1.26 [1]	0.989 [7]	5.60E+00 [1]	46.69 [1]	21.6	220.3 [1]
320	n-pentanol	88.15	195.0 [1]	411.1 [1]	588.2 [1]	0.8124 [1]	108.5	0.89 [1]	0.884 [1]	3.15E-01 [1]	57.02 [1]	22.4	208.9 [1]

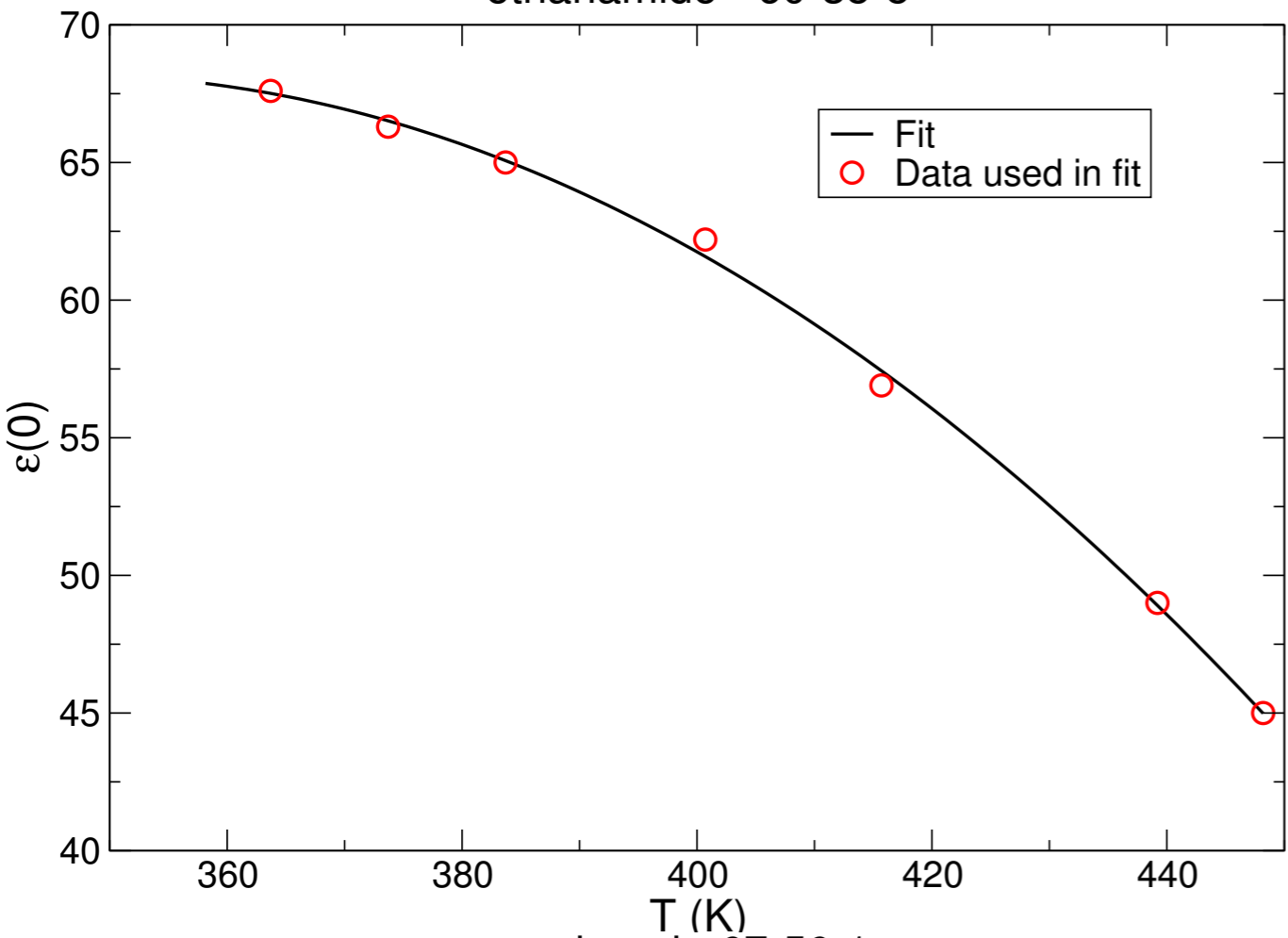
# Handbook of Chemistry & Physics



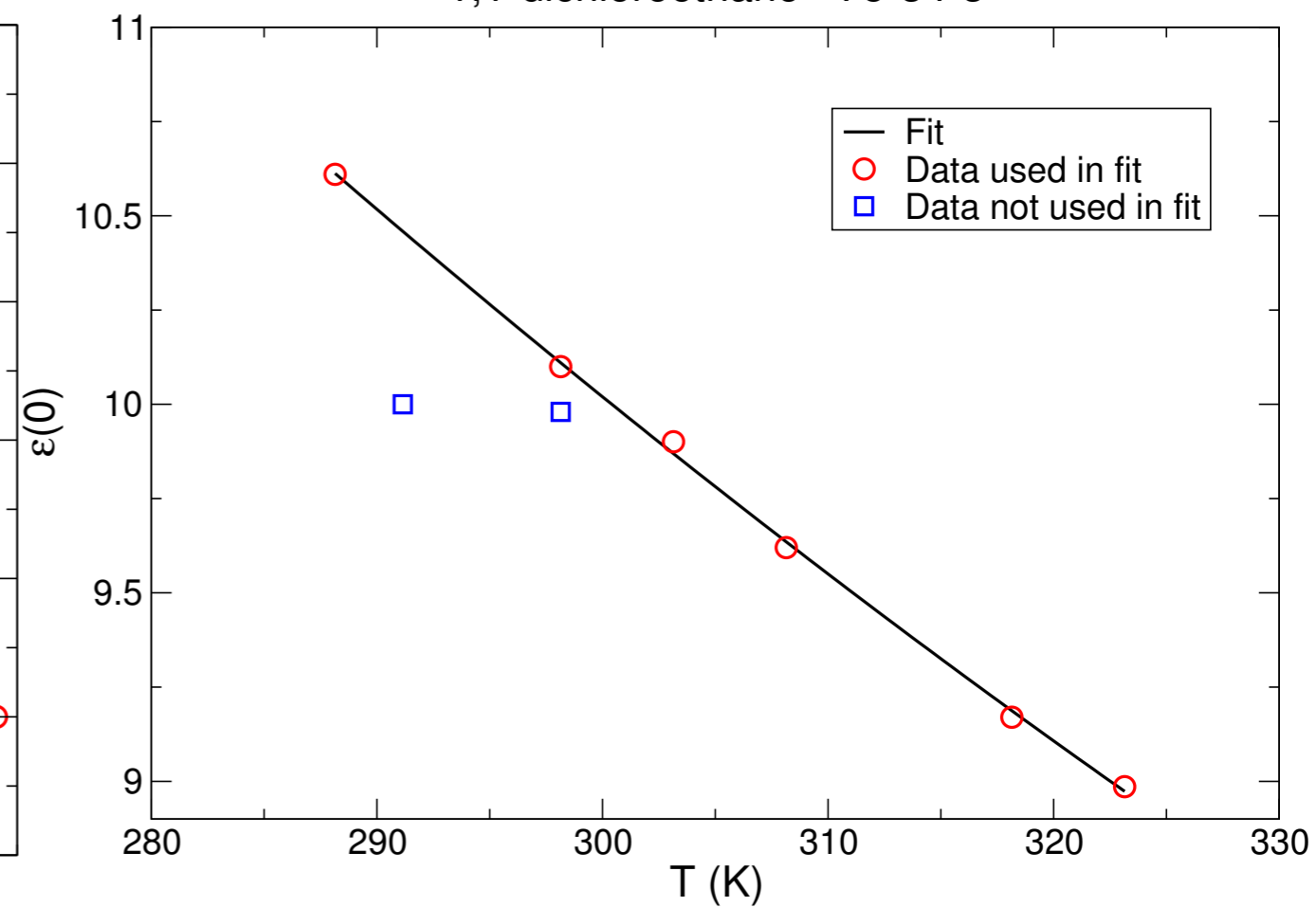


Science in the 21<sup>st</sup> century...

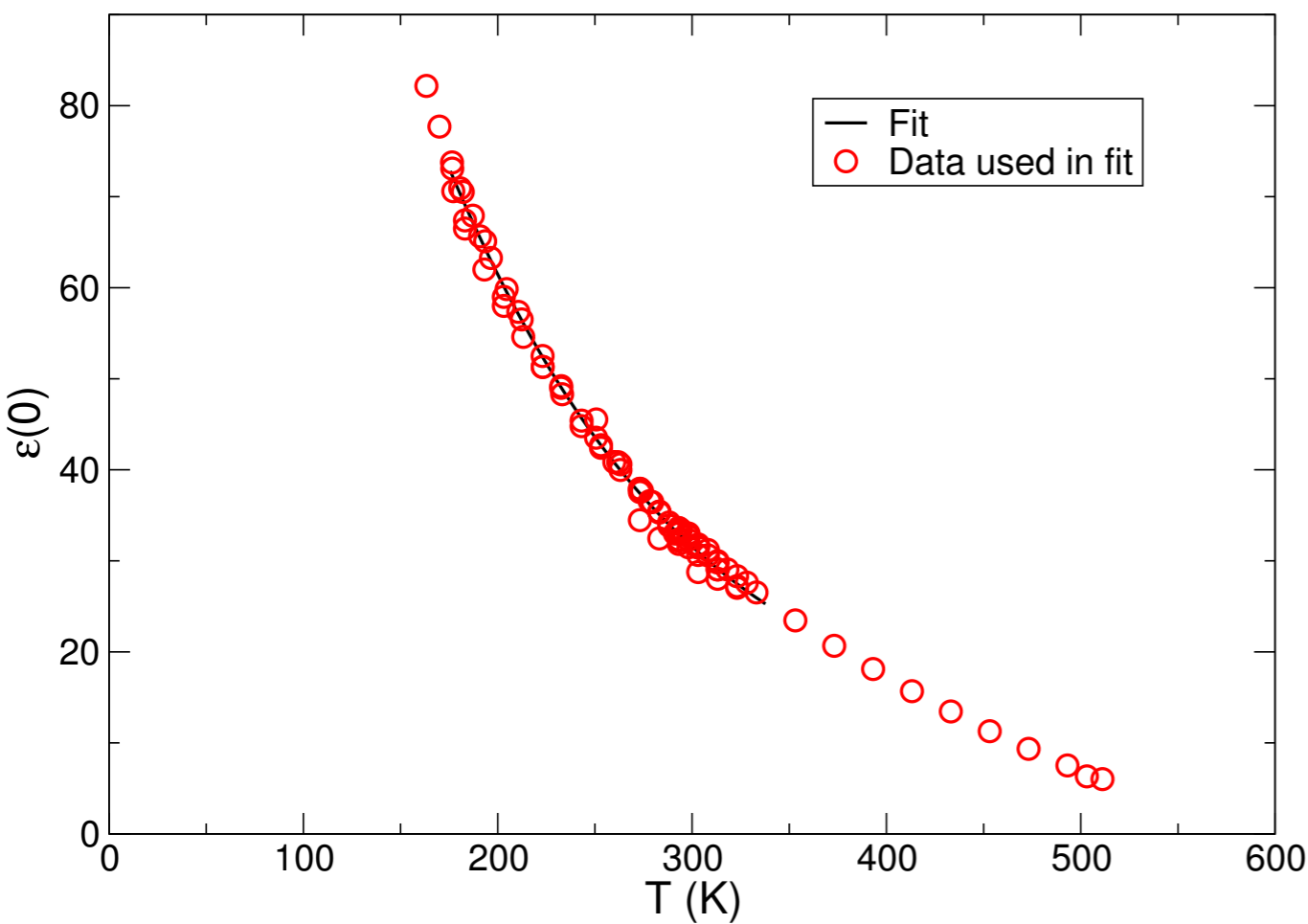
ethanamide - 60-35-5



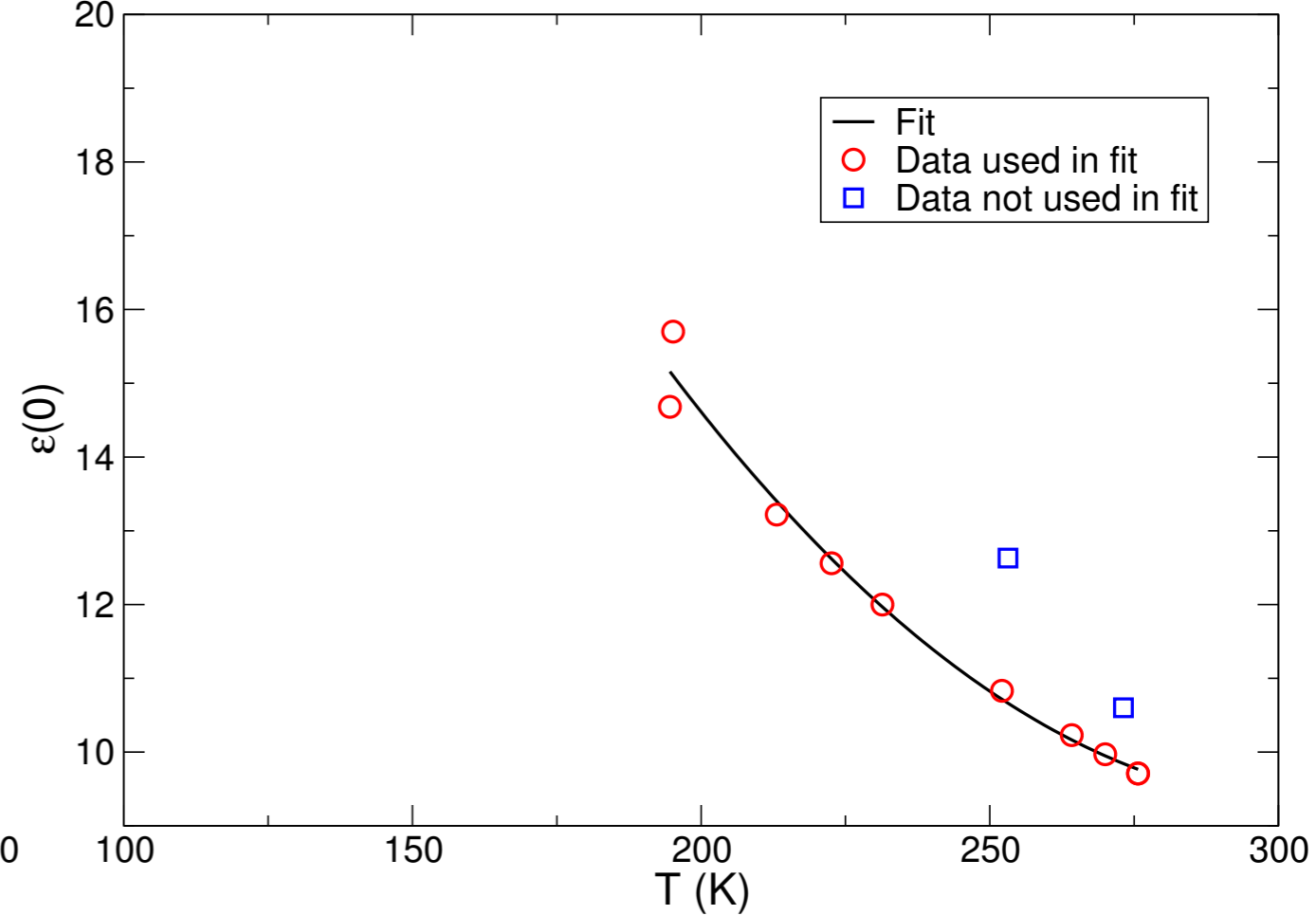
1,1-dichloroethane - 75-34-3



methanol - 67-56-1



bromomethane - 74-83-9



Force field	N	a	b	RMSD	% Dev.	$R^2$
$\rho$ (g/l)						
GAFF	235	0.96	58.6	82.9	4	97%
OPLS/AA	235	0.98	21.3	40.3	2	99%
CGenFF <sup>36</sup>	111	1.03	-36.0	26.0	2	99%
OPLS/AA <sup>70</sup>	9	1.01	-24.0	45.3	4	96%
$\Delta H_{\text{vap}}$ (kJ/mol)						
GAFF	231	1.07	0.8	10.6	17	83%
OPLS/AA	231	0.96	3.4	6.5	11	89%
CGenFF <sup>36</sup>	95	0.94	2.4	4.7	7	84%
$\gamma$ ( $10^{-3}$ N/m)						
GAFF	155	0.75	0.9	8.6	23	70%
OPLS/AA	155	0.97	-5.5	7.3	22	89%
$\epsilon(0)$						
GAFF	170	0.21	0.6	23.4	52	48%
OPLS/AA	183	0.16	0.7	22.7	57	56%
$\alpha_P$ ( $10^{-3}$ /K)						
GAFF	221	0.90	0.3	0.3	24	67%
OPLS/AA	221	0.91	0.3	0.3	21	75%
OPLS/AA <sup>70</sup>	9	0.53	0.8	0.7	42	39%
$\kappa_T$ (1/GPa)						
GAFF	60	0.56	0.1	0.3	31	64%
OPLS/AA	60	0.61	0.2	0.3	21	76%
OPLS/AA <sup>70</sup>	8	0.93	0.0	1.1	59	84%

# Statistics

- Quantitative evaluation per property.

# Benchmark is Foundation for Future FF

- > 100,000 experimental data points gathered in a SQL database
- Allows rational FF derivation ... at last

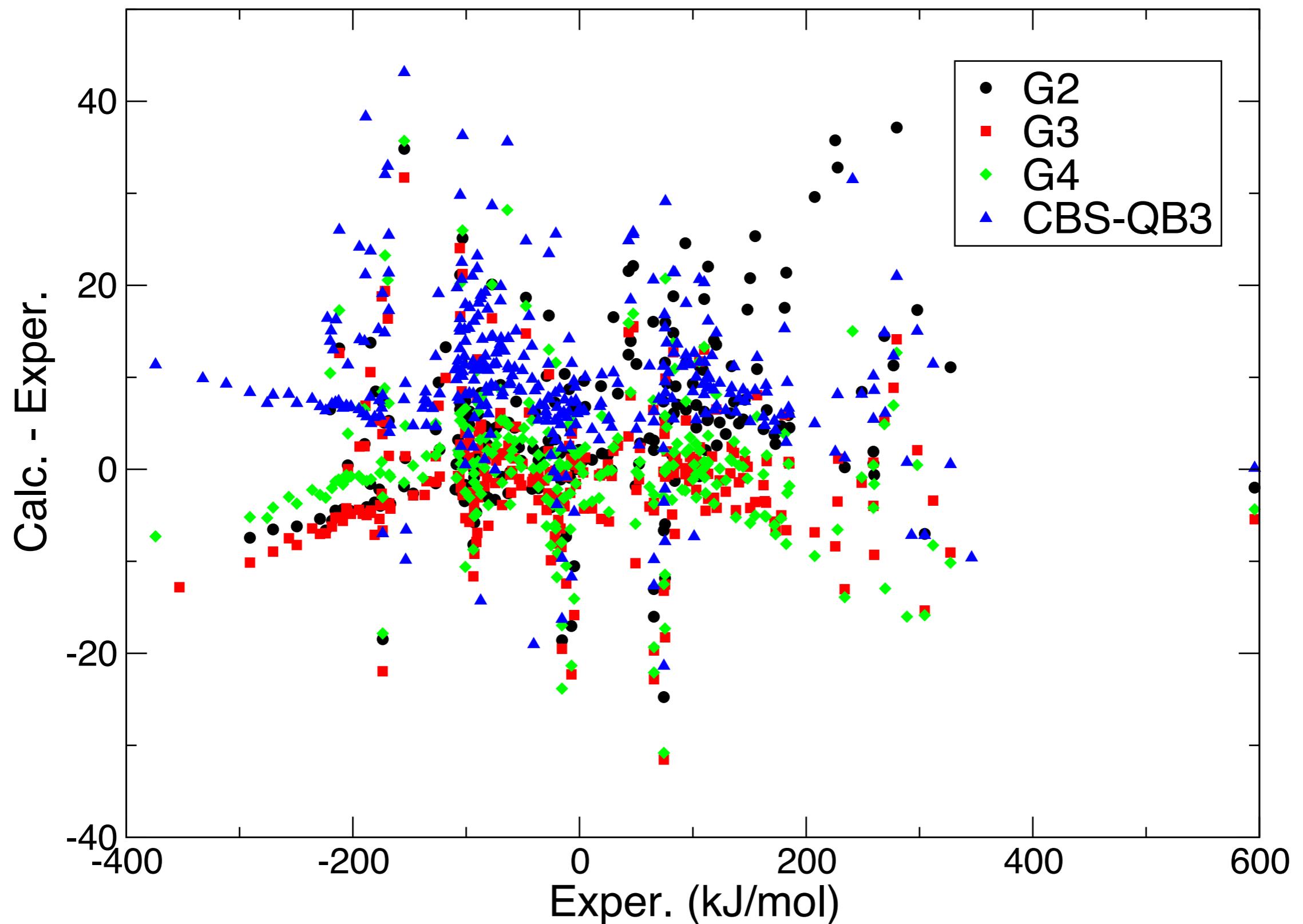


<http://virtualchemistry.org/>

# Can Quantum Chemistry Help?

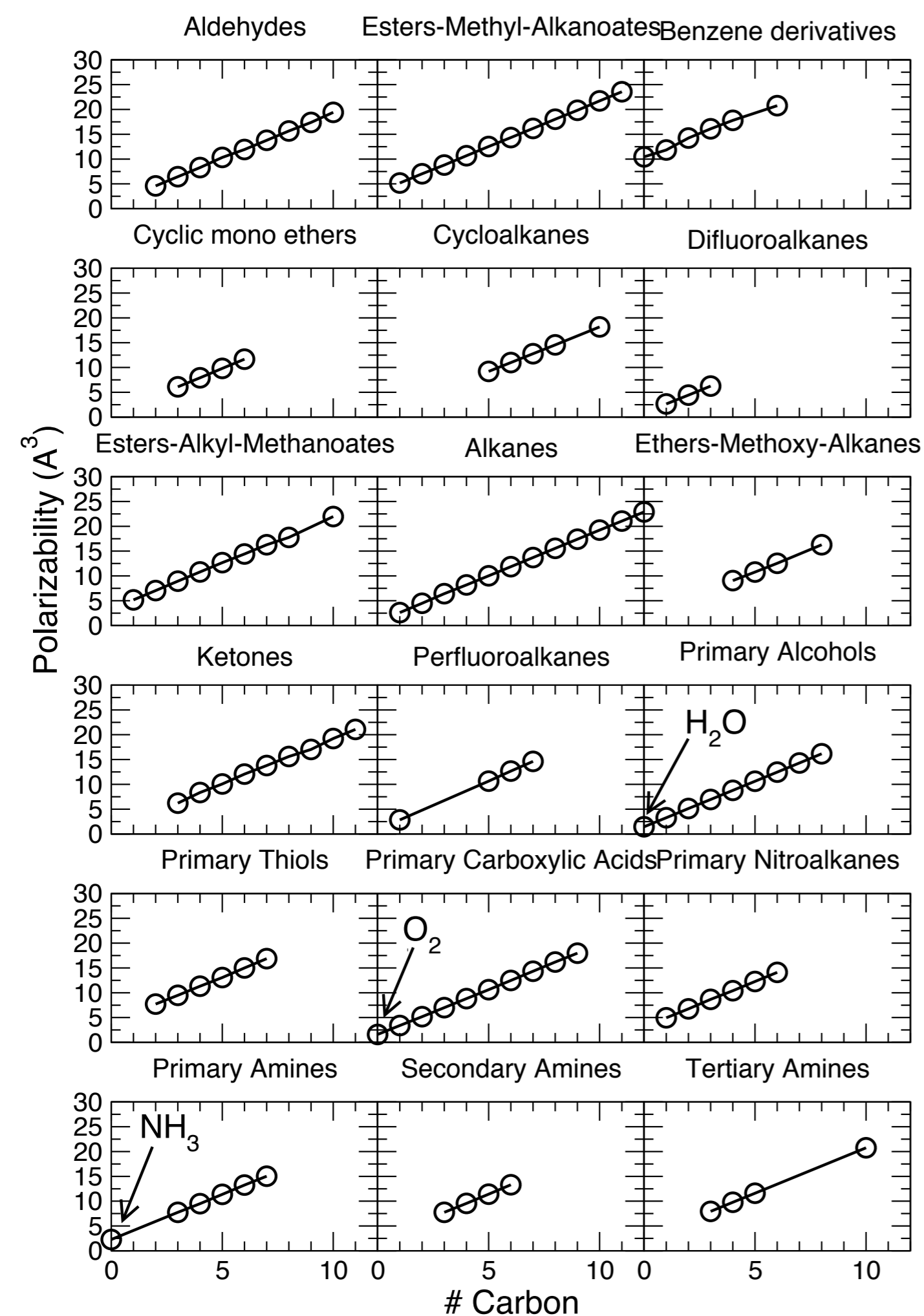
- Compute properties for which there is no experimental data
- Electric properties (multipole moments) polarizabilities are reproduced well
- Energies ?

# Enthalpy of Formation



# Fear not

- Nature is linear...



# Summary Force Field

- Intermolecular energies within  $\sim 5\text{-}7$  kJ/mol in force fields - for supported atom types
- A lot of work going on in force field tuning and development
- Many properties can be computed based on long classical simulations

# References

- Carl Coleman, Paul van Maaren, Minyan Hong, Jochen Hub, Luciano Costa, David van der Spoel, J. Chem.Theor. Comput. 8 (2012) 61-74
- David van der Spoel, Paul van Maaren, Carl Coleman, Bioinformatics (2012) doi: 10.1093/bioinformatics/bts020
- Oliver Lange, David van der Spoel, Bert L. de Groot - Biophysical Journal 99 (2010) 647-655

# The Two Phase Thermodynamics Method



David van der Spoel, Uppsala University

# What's the problem?

- For ideal gases theories exist from which one can derive thermodynamics properties
- For solids another kind of theory exists
- For liquids there is no such thing

# 1<sup>st</sup> Ansatz

- Treat Liquid just like a Solid - system of harmonic oscillators

## II. CLASSICAL THERMODYNAMICS FROM MOLECULAR DYNAMICS

The standard equations<sup>1</sup> linking the canonical partition function  $Q$  and the various thermodynamic variables are

$$E = k_B T^2 \frac{\partial \ln Q}{\partial T} , \quad (2.1)$$

$$C_v = \frac{\partial E}{\partial T} , \quad (2.2)$$

$$A = -k_B T \ln Q , \quad (2.3)$$

$$S = k_B T \frac{\partial \ln Q}{\partial T} + k_B \ln Q , \quad (2.4)$$

in which  $E$  is the energy,  $C_v$  the constant volume heat capacity,  $A$  the Helmholtz free energy,  $S$  the entropy,  $k_B$  Boltzmann's constant, and  $T$  the temperature.

Berens et al. JCP 79 (1983) pp2375

In the harmonic limit, a normal mode analysis allows us to view the system as a set of  $3N$  harmonic oscillators. The total canonical partition function  $Q$  for the system can then be expressed in terms of the partition functions  $q_j$  for the individual modes as

$$Q = \prod_{j=1}^{3N} q_j \quad (3.18)$$

or

$$\ln Q = \sum_{j=1}^{3N} \ln q_j . \quad (3.19)$$

If the normal frequencies are continuously distributed we may take the integral

$$\ln Q = \int_0^{\infty} d\nu S(\nu) \ln q(\nu) , \quad (3.20)$$

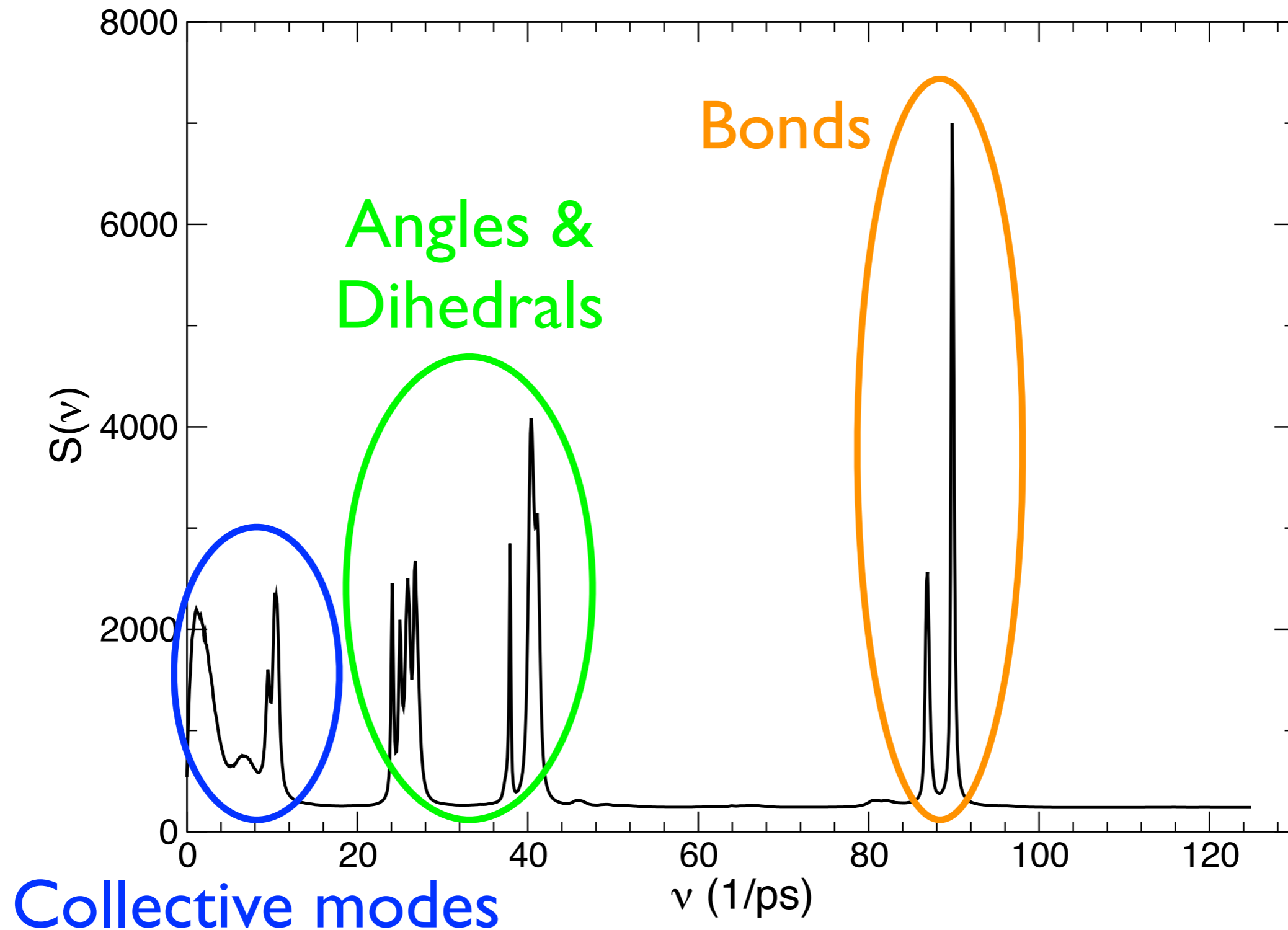
where  $S(\nu)$  is the density of normal modes with frequency  $\nu$ .

Berens et al. JCP 79 (1983) pp2375

# The trick

- $S(v)$  can be derived from the velocity auto-correlation function
- Assume the frequencies in the classical simulation are correct (and the amplitudes)
- Reweigh the  $S(v)$  to get a corresponding Quantum  $S(v)$

# Example - C<sub>2</sub>H<sub>6</sub>SO



Now we will try to comprehend the solid component of the density of states,  $DoS_{\text{solid}}(\nu)$ . Here, each mode is considered to be harmonic and we use the partition function for a quantum harmonic oscillator as given by McQuarrie [8]:

$$q_{\text{HO}}^q(\nu) = \frac{e^{-\beta h\nu/2}}{1 - e^{-\beta h\nu}} \quad (\text{S9})$$

where  $h$  is Planck's constant,  $\beta = 1/k_{\text{B}}T$ . Since the canonical partition function  $Q$  of a system is given by the product of the components (Equations 3.18-3.20, reference [6]):

$$Q = \prod_{i=1}^N q_i \quad (\text{S10})$$

and therefore

$$\ln Q = \sum_{i=1}^N \ln q_i \quad (\text{S11})$$

**Caleman et al. JCTC 8 (2012) 61-74**

# Final Result I

$$E^Q = V_0 + k_B T \int_0^\infty d\nu S(\nu) W_E^Q(\nu) ; \quad W_E^Q(\nu) = \left( \frac{u}{2} + \frac{u}{e^u - 1} \right) , \quad (3.40)$$

$$C_v^Q = k_B \int_0^\infty d\nu S(\nu) W_{C_v}^Q(\nu) ; \quad W_{C_v}^Q(\nu) = \left( \frac{u^2 e^u}{(1 - e^u)^2} \right) , \quad (3.41)$$

$$A^Q = V_0 + k_B T \int_0^\infty d\nu S(\nu) W_A^Q(\nu) ; \quad W_A^Q(\nu) = \left( \ln \frac{1 - e^{-u}}{e^{-u/2}} \right) , \quad (3.42)$$

$$S^Q = k_B \int_0^\infty d\nu S(\nu) W_S^Q(\nu) ; \quad W_S^Q(\nu) = \left( \frac{u}{e^u - 1} - \ln(1 - e^{-u}) \right) . \quad (3.43)$$

Berens et al. JCP 79 (1983) pp2375

# 2<sup>nd</sup> Ansatz

- Treat a liquid as a combination of solid and ideal gas - 2 phase thermodynamics
- Gas can be treated as a hard-sphere gas for which analytical thermodynamical results exist

Lin et al. JCP 2003, JPCB 2012, Pascal PCCP 2011

# Final Result 2

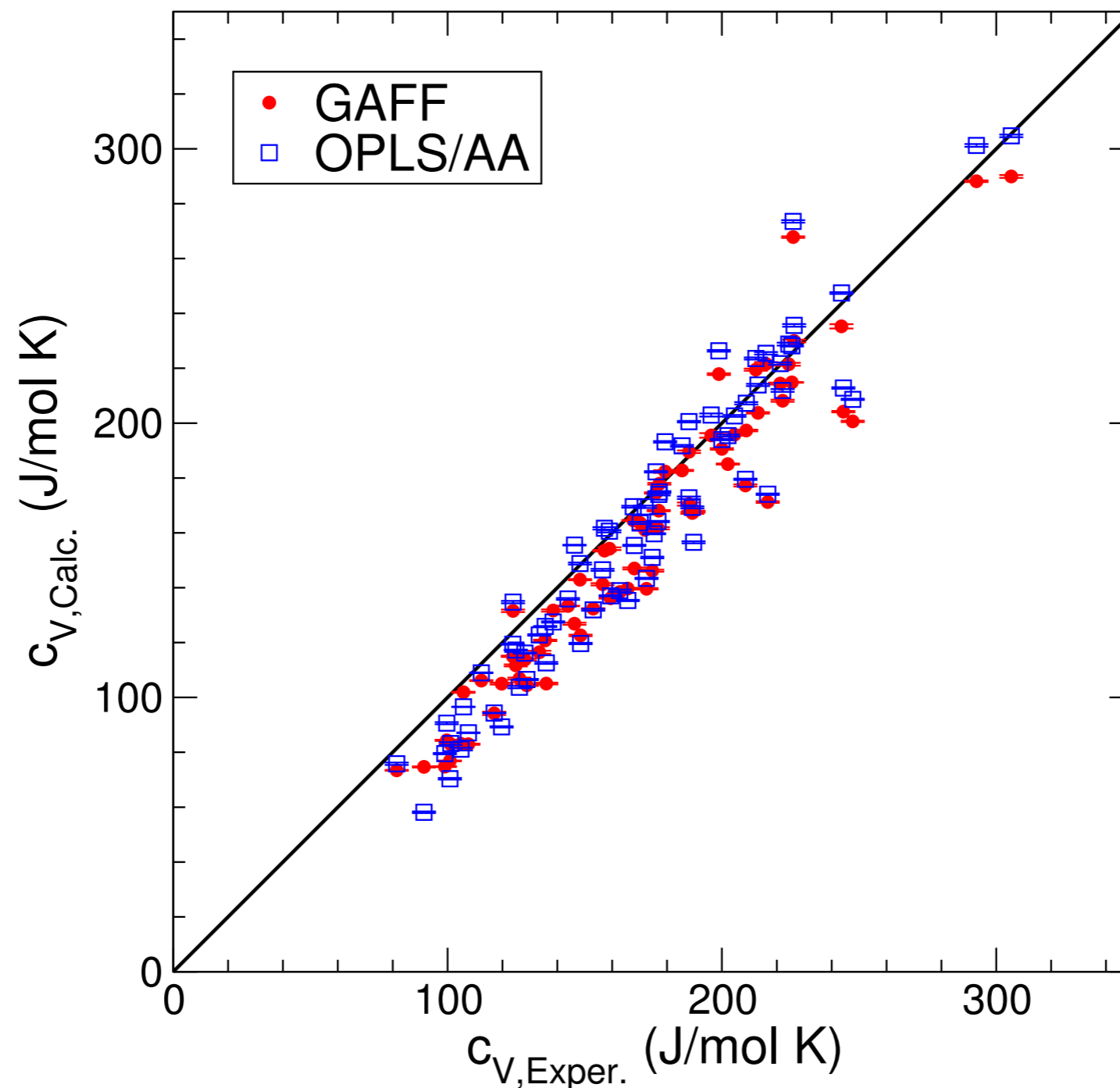
- Determine “fluidicity” - how fluid is the simulation between 0 and 1
- Modified weighting function - same as Berens for the solid part + another for the gas part

Lin et al. JCP 2003, JPCB 2012, Pascal PCCP 2011

# How does it work?

- Do MD simulation with flexible bonds, 20-100 ps (time step 0.2 fs)
- Save velocities every 4-5 fs
- Compute mass-weighted velocity ACF and compute properties  $S$ ,  $E$ ,  $A$ ,  $C_v$  by weighting the  $S(v)$  and integrating!

# Heat Capacity $C_v$

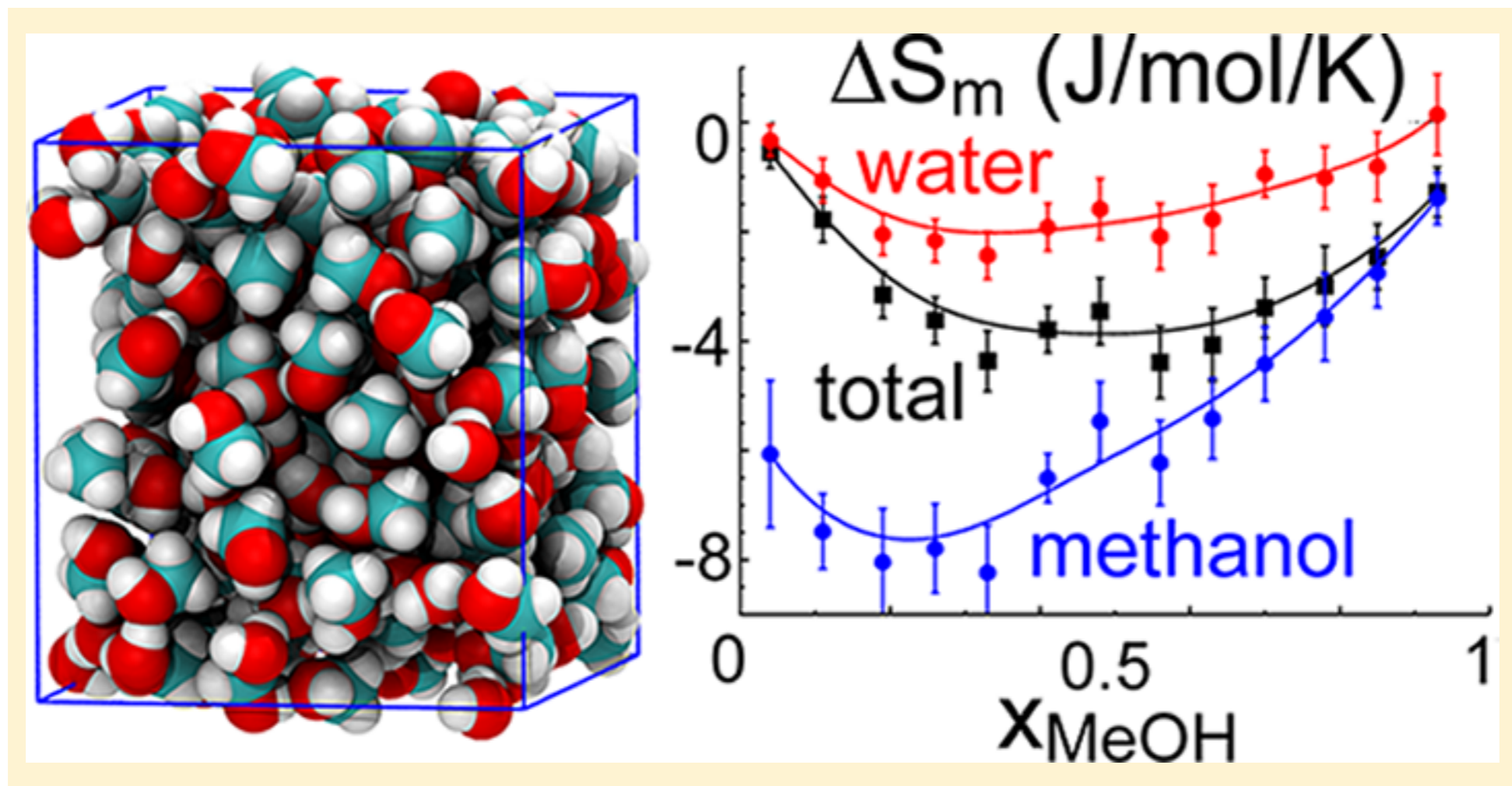


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# Hydrophobic Segregation, Phase Transitions and the Anomalous Thermodynamics of Water/Methanol Mixtures

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# Summary 2PT

- Promising new method
- Lowest frequencies contribute most - may also work with constraints
- Very recently also for mixtures
- More development and testing needed

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